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# Phase relation studies in  $Pb_{1-x}M'_{x}F_{2+x}$  systems  $(0.0 \le x \le 1.0;$  $M' = Nd^{3+}$ ,  $Eu^{3+}$  and  $Er^{3+}$ )

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#### Abstract

In this communication we report the synthesis and characterization of a series of compounds with the general composition  $Pb_{1-x}M'_{x}F_{2+x}$ ,  $(0.0 \le x \le 1.0; M' = Nd^{3+}, Eu^{3+}$  and  $Er^{3+})$  to elucidate the detailed phase relations between  $PbF_{2}$  and  $M'F_{3}$ . These three rare-earth fluorides were selected so as to delineate the effect of ionic size on the phase relations. In all the three systems, fluorite-type solid solutions are formed at the PbF<sub>2</sub> rich end. The solid solubility limits of NdF<sub>3</sub>, EuF<sub>3</sub> and ErF<sub>3</sub> in the PbF<sub>2</sub> lattice, as observed from this study, are 30, 25 and 15 mol%, respectively. In  $PbF_2-NdF_3$  system, beyond the fluorite-type solid solutions, NdF<sub>3</sub> phase is observed. However, in both PbF<sub>2</sub>–EuF<sub>3</sub> and PbF<sub>2</sub>–ErF<sub>3</sub> systems, certain fluorite related ordered phases, namely, a rhombohedral phase with about 40 mol% of  $EuF_3$  or  $ErF_3$  in PbF<sub>2</sub>, and a tetragonal phase with 45–50 mol% of  $ErF_3$  in PbF<sub>2</sub>, are observed. In all the three systems, no solubility of the  $PbF_2$  in the hexagonal or orthorhombic rare-earth fluoride lattice is observed. This is the first report on phase relation in these three systems under short annealed and slow cooled condition.  $O$  2004 Elsevier Inc. All rights reserved.

Keywords: Fluorides; X-ray diffraction; Phase equilibria

### 1. Introduction

The fluorite-type  $PbF_2(\beta)$  and  $PbF_2$  containing compounds have drawn a significant interest owing to their superionic properties [\[1\].](#page-10-0) The presence of frenkel anions in addition to a lone pair on  $Pb^{2+}$  makes them superior fluoride ion conductors compared to other fluorite-type fluorides, e.g., alkaline-earth fluorides [\[2\]](#page-10-0). Besides, the presence of lone pair, lower melting point of  $PbF<sub>2</sub>$  further facilitates the anion migration in the lattice. The ionic conductivity can be further enhanced by increasing the defects in the lattice. It was also reported that the ionic conduction of the  $PbF_2$  could be significantly modified with non-stoichiometry created by aliovalent cation (viz.  $M^{3+}$  ions) substitution in place of  $Pb^{2+}$  [\[3–6\]](#page-10-0). PbF<sub>2</sub> is highly prone to hydrolysis and also it has more affinity towards oxygen than fluorine. Thus, it is widely used as the deoxidizer in the growth of high purity crystals of various rare-earth fluorides and also to remove even the last traces of oxygen in the fluoride melt [\[7\]](#page-10-0). Due to its low melting and boiling points it can be

removed easily leading to high purity crystals. Besides,  $PbF_2$  and  $CdF_2$  have been widely used in the preparation of transparent glass ceramic in lead-based glass systems, owing to the easier crystallization of the cubic PbF<sub>2</sub> or CdF<sub>2</sub> phases [\[8–10\].](#page-11-0) The segregation of rareearth-doped ceramic phase in the transparent glass matrix poses interesting optical applications. The composition of the segregated phase in the glass matrix can be easily identified from the XRD data, if the XRD details of the corresponding pure crystalline phases are available on hand. Mortier et al. [\[9\]](#page-11-0) have used such methods to identify the crystalline phases from the powder XRD data and based on that they explained their optical properties of glass ceramics. Therefore, it is important to investigate the crystalline phases in mixed fluoride systems from the point of view of characterization of optical transparent glass ceramics also. In order to know the maximum possible non-stoichiometric phases and the formation of various probable ordered phases, the phase relation in  $PbF_2-MF_3$  systems is used as an essential source of information. Thus, fluorite-type solid solutions in several of  $PbF_2-M'F_3$  (*M*<sup> $\prime$ </sup> = rare-earth ions) systems have been investigated under various experimental conditions [\[11–16\].](#page-11-0) However, to get the

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reliable data on  $PbF_2$ -based systems, which are prone to hydrolysis, a short annealing condition needs to be optimized. Hence, it is worthwhile to investigate the existing and probable new phases with the rare-earth fluorides and  $PbF_2$  under a short annealing condition. The detail results will also be useful in identifying the crystalline phase in partially crystallized lead-based fluoride or oxy-fluoride glass ceramics.

It is well known that the rare-earth fluorides crystallize in two different modifications, namely, hexagonal (tysonite) or orthorhombic  $(\beta$ -YF<sub>3</sub>) structure depending on the ionic radii [\[17\].](#page-11-0) The lighter rare-earths fluorides  $(LaF_3$  to PmF<sub>3</sub>) have the hexagonal lattice whereas the heavier rare-earth fluorides (GdF<sub>3</sub> to  $LuF_3$  including the  $YF_3$ ) have the orthorhombic lattice. It is also reported that  $SmF_3$  and  $EuF_3$  exist in both types of structures depending upon the method of preparation. For the present study, the above-mentioned typical lattice types are represented by  $NdF_3$ , EuF<sub>3</sub> and ErF<sub>3</sub>. This study is aimed at delineating the role of structure type of  $M'F_3$ and ionic radii of the rare-earth ions on the phase width of the fluorite-type solid solutions and the ordering of the non-stoichiometric phases.

PbF<sub>2</sub> exists in orthorhombic  $(\alpha)$  modification at room temperature and undergoes an irreversible phase transition to cubic-fluorite type structure [\[18\].](#page-11-0) Earlier, the unit cell details of some fluorite type solid solution compositions in  $PbF_2-Err_3$  system were reported in the context of identification of ceramic phase in  $Erf_3$  containing  $50GeO<sub>2</sub>$ -40PbO-10PbF<sub>2</sub> glasses [\[9\].](#page-11-0) A complete phase diagram in the PbF<sub>2</sub>–YF<sub>3</sub> system had been given by Reau et al. [\[11\]](#page-11-0). They had reported the existence of three different types of phases, namely, fluorite-type solid solution, a rhombohedral phase similar to  $A_4B_3F_{17}$  $(A=ST^{2+}, Ba^{2+}; B=RE^{3+})$  as reported by Kaiser et al. [\[19\]](#page-11-0), Sobolev and his coworkers [\[20\].](#page-11-0) Also, they reported a phase with composition  $PbYF_5$  at lower temperatures. At higher temperatures they obtained a tysonite type phase at about 75 mol% of  $YF_3$  and 25 mol% of PbF<sub>2</sub>, which is stable only in a narrow temperature range. Subsequent study [\[12\]](#page-11-0) on the phase relation on  $PbF_{2}$  $M<sup>T</sup>$ <sub>3</sub> revealed that there are three different type phases, namely, fluorite-type solid solution,  $A_4B_3F_{17}$  type phase and a tetragonal phase at composition of  $Pb_2YF_7$ . Sobolev and his coworkers had also published phase diagrams in  $PbF_2-M'F_3$ ,  $M' =$ Lanthanides, Y and Sc [\[13–15\]](#page-11-0). However, in their studies they mentioned only about the fluorite-type solid solution and  $A_4B_3F_{17}$  type phases. According to them the  $A_4B_3F_{17}$  phase exists in a narrow composition range ( $\pm$ 1.5 mol% of M'F<sub>3</sub>). They did not observe any tetragonal phase in their series. In a short annealed study of  $PbF_2-YF_3$  system [\[16\],](#page-11-0) it was found that the fluorite-type solid solution (up to 22 mol% of  $YF_3$ ) and a rhombohedral  $Pb_4Y_3F_{17}$ compound exist [\[21\]](#page-11-0). A pseudo-tetragonal phase was observed near the composition close to 50 mol% of  $YF_3$  in PbF<sub>2</sub>. In case of  $M' = Sc^{3+}$ , only cubic solid solution and after the saturation limit, separation of  $\text{SCF}_3$  was observed. A comparison of earlier reported phase relations of  $M\text{F}_2$ - $M'\text{F}_3$  ( $M$  = Ca, Ba and Sr;  $M'$  = rareearth ions) systems with the  $PbF_2-M'F_3$  systems, indicate that although ionic radii of  $Pb^{2+}$  (1.29 Å) is very close to that of  $Sr^{2+}$  (1.26 Å), PbF<sub>2</sub> behaves differently from  $SF_2$ , due to the lone pair on  $Pb^{2+}$ . The present study is carried out under short annealing and slow cooling condition and the results will supplement to the earlier reports on the phase relation in  $PbF_2$  and  $M'F_3$  systems.

## 2. Experimental

The starting materials  $NdF_3$  and  $EuF_3$  were synthesized by repeatedly heating  $Nd_2O_3$  and  $Eu_2O_3$ with excess of  $NH_4HF_2$ . The  $\alpha$ -PbF<sub>2</sub> (Merck) and  $\beta$ -ErF<sub>3</sub> (Fluka) were dried before the use. Three series of nominal compositions with stoichiometry  $Pb_{1-x}M'_{x}F_{2+x}$  (0.00 \eta \alumin \alumin \alumin \alumin M' = Nd<sup>3+</sup>, Eu<sup>3+</sup> and  $Er^{3+}$ ) were prepared. About 300 mg of each mixture was pressed into a pellet of 6 mm diameter, wrapped in a platinum foil and sealed in an evacuated quartz tube. The tube was heated to  $650^{\circ}$ C at the rate of  $4^{\circ}$ C/min and held there for 4h. The samples were cooled back to room temperature at a rate of  $2^{\circ}C/\text{min}$ . The powder XRD patterns of the products were recorded on a Philips (PW1710 model) X-ray diffractometer with Nifiltered Cu-K $\alpha$  radiation. The detailed phase analyses of the three systems are explained in the following section.

## 3. Results and discussion

It was mentioned in the introduction that the metastable orthorhombic modification of  $PbF<sub>2</sub>$  transforms irreversibly to the cubic fluorite form at about  $350^{\circ}$ C. Thus, at the preparation temperature adopted in the present study, the orthorhombic structure of  $PbF<sub>2</sub>$ transformed to the cubic structure. From the XRD data of the nominal composition  $Pb_{1-x}M'_{x}F_{2+x}$  (for  $x = 1.0$ ), it was observed that NdF<sub>3</sub> has retained the hexagonal tysonite-type lattice and  $EuF_3$  and  $ErF_3$  have retained the orthorhombic lattice after the heat treatment. The low melting and superionic nature of the cubic  $PbF_2$  makes the reaction fast enough to go for completion in a short time compared to alkaline-earth fluorides.

The further nominal compositions in the series  $Pb_{1-x}M'_{x}F_{2+x}$  (0.00  $\leq x \leq 1.00$ ;  $M' = Nd^{3+}$ , Eu<sup>3+</sup> and  $Er<sup>3+</sup>$ ) are characterized by comparing the successive XRD patterns of the respective series. The unit cell parameters of various phases are determined by indexing the observed reflections. Various phases identified in

these three systems are presented in Tables 1–3. The systematic phase analyses of various nominal compositions prepared in three systems of  $PbF_2-M'F_3$  $(M' = Nd^{3+}$ , Eu<sup>3+</sup> and Er<sup>3+</sup>) are summarized in [Table 4](#page-5-0). The  $PbF_2-M'F_3$  systems can be grouped into three phase-regions, namely, a fluorite-type solid solution, fluorite related ordered phases and the rare-earth fluorides.

A comparison of the XRD patterns of the compositions  $Pb_{1.00}M'_{0.00}F_{2.00}$   $(M' = Nd^{3+}, Eu^{3+}$  and  $Er^{3+})$ with those of the successive compositions in the respective series revealed their close similarity, indicating the solid solution formation up to a certain extent. However, the peak positions shift towards the higher angle side as the  $M/F_3$  contents in the compositions increases, implying the contraction of the lattice. The solid solution formation was observed up to the nominal compositions  $Pb_{0.70}Nd_{0.30}F_{2.30}$ ,  $Pb_{0.75}Eu_{0.25}F_{2.25}$  and  $Pb_{0.85}Er_{0.15}F_{2.15}$  in the respective series. The typical XRD patterns for the respective solid solution limits are shown in [Fig. 1.](#page-6-0)

The solid solution of the fluorite-type lattice is the most common observation in the  $MF_2-M'F_3$  ( $M = \text{alka}$ line-earth cation and  $M'$  = rare-earth cation) systems [\[22\]](#page-11-0). These solid solutions have been explained with the anion-excess fluorite lattice [\[23,24\].](#page-11-0) The  $Pb^{2+}$  and the rare-earth ions are expected to be statistically distributed over the 4a site of the space group Fm3m. The excessanions occupy the interstitial sites available in the fluorite lattice, namely, 32f (xxx, for  $x = 0.40$ ) and 48i (1/2 x x, for  $0.35 \le x \le 0.40$ ) sites [\[23\].](#page-11-0) In the solid solution formation the inter-anionic repulsion can also displace some of the regular lattice site  $(8c)$  anions to these interstitial sites. Thus anions are distributed in the 8c; 48i and 32f sites forming a 222-type cluster. It can be emphasized here that even in the fluorite-type solid solution region the short-range anion clusters should not be ignored. Several reports dealing with the structural analyses show the presence of 222 type clusters in lower concentration of the  $M'F_3$ , whereas the presence of 432, 443 type clusters in the regions with higher concentration of the  $M'F_3$  [\[23–26\]](#page-11-0).

Table 1

Nominal compositions and their phase relations in  $Pb_{1-x}Nd_xF_{2+x}$ 

S. No.	Nominal composition	mol% of $NdF_3$	Phase $(s)$ present	$a(\AA)$	$b(\AA)$	$c(\AA)$	$V(\AA)^3$
1	$Pb_{1.00}Nd_{0.00}F_{2.00}$	$\boldsymbol{0}$	$\mathbf C$	5.942(1)	5.942(1)	5.942(1)	209.81(4)
$\mathfrak{2}$	$Pb_{0.95}Nd_{0.05}F_{2.05}$	5	${\bf C}$	5.937(0)	5.937(0)	5.937(0)	209.23(3)
3	$Pb_{0.90}Nd_{0.10}F_{2.10}$	10	C	5.927(0)	5.927(0)	5.927(0)	208.21(2)
4	$Pb_{0.85}Nd_{0.15}F_{2.15}$	15	C	5.921(0)	5.921(0)	5.921(0)	207.58(2)
5	$Pb_{0.80}Nd_{0.20}F_{2.20}$	20	C	5.917(1)	5.917(1)	5.917(1)	207.16(1)
6	$Pb_{0.75}Nd_{0.25}F_{2.25}$	25	C	5.905(0)	5.905(0)	5.905(0)	205.90(3)
7	$Pb_{0.70}Nd_{0.30}F_{2.30}$	30	C	5.895(1)	5.895(1)	5.895(1)	204.87(6)
8	$Pb_{0.65}Nd_{0.35}F_{2.35}$	35	$\mathbf C$	5.895(0)	5.895(0)	5.895(0)	204.87(2)
			H	a			
9	$Pb_{0.60}Nd_{0.40}F_{2.40}$	40	$\mathbf C$	5.895(1)	5.895(1)	5.895(1)	204.86(7)
			H	7.039(5)	7.039(5)	7.218(6)	309.7(4)
10	$Pb_0$ 55 $Nd_0$ 45 $F_2$ 45	45	${\bf C}$	5.892(0)	5.892(0)	5.892(0)	204.50(2)
			H	7.033(4)	7.033(4)	7.187(5)	307.9(3)
11	$Pb_{0.50}Nd_{0.50}F_{2.50}$	50	${\bf C}$	5.890(0)	5.890(0)	5.890(0)	204.32(3)
			H	7.034(2)	7.034(2)	7.195(4)	308.3(2)
12	$Pb_{0.45}Nd_{0.55}F_{2.55}$	55	${\bf C}$	5.892(1)	5.892(1)	5.892(1)	204.60(3)
			H	7.038(2)	7.038(2)	7.209(4)	309.2(2)
13	$Pb_{0.40}Nd_{0.60}F_{2.60}$	60	${\bf C}$	5.892(0)	5.892(0)	5.892(0)	204.49(3)
			H	7.038(2)	7.038(2)	7.199(2)	308.8(2)
14	$Pb_{0.35}Nd_{0.65}F_{2.65}$	65	${\bf C}$	5.895(1)	5.895(1)	5.895(1)	204.87(7)
			H	7.037(2)	7.037(2)	7.198(2)	308.7(1)
15	$Pb_{0.30}Nd_{0.70}F_{2.70}$	70	${\bf C}$	5.895(2)	5.895(2)	5.895(2)	204.84(10)
			H	7.037(3)	7.037(3)	7.207(3)	309.1(2)
17	$Pb_{0.25}Nd_{0.75}F_{2.75}$	75	${\bf C}$	5.893(6)	5.893(6)	5.893(6)	204.7(3)
			H	7.035(1)	7.035(1)	7.198(2)	308.5(1)
19	$Pb_{0.20}Nd_{0.80}F_{2.80}$	80	${\bf C}$	5.888(6)	5.888(6)	5.888(6)	204.2(4)
			H	7.027(2)	7.027(2)	7.196(3)	307.8(2)
21	$Pb_{0.15}Nd_{0.85}F_{2.85}$	85	${\bf C}$	5.896(6)	5.896(6)	5.896(6)	205.0(4)
			H	7.033(1)	7.033(1)	7.204(1)	308.6(1)
24	$Pb_{0.10}Nd_{0.90}F_{2.90}$	90	${\bf C}$	5.90(1)	5.90(1)	5.90(1)	205.3(6)
			H	7.040(2)	7.040(2)	7.208(2)	309.4(2)
25	$Pb_{0.05}Nd_{0.95}F_{2.95}$	95	$\mathsf{C}$	$\rm{a}$			
			H	7.033(1)	7.033(1)	7.198(1)	308.33(8)
25	$Pb_{0.00}Nd_{1.00}F_{3.00}$	100	H	7.028(1)	7.028(1)	7.196(1)	307.8(1)

 $C =$ Cubic (fluorite) type,  $H = NdF_3$  (hexagonal tysonite-type).<br><sup>a</sup>Corresponding phases were not refined due to very insignificant intensities of reflections

Table 2 Nominal compositions and their phase relations in  $Pb_{1-x}Eu_{x}F_{2+x}$ 

S. No.	Nominal composition	mol% of $EuF_3$	Phase(s) present	$a(\AA)$	b(A)	$c(\AA)$	$V(\AA)^3$
$\mathbf{1}$	$Pb_{1.00}Eu_{0.00}F_{2.00}$	$\boldsymbol{0}$	$\mathbf C$	5.939(1)	5.939(1)	5.939(1)	209.51(3)
$\overline{c}$	$Pb_{0.95}Eu_{0.05}F_{2.05}$	5	$\mathbf C$	5.928(1)	5.928(1)	5.928(1)	208.28(4)
3	$Pb_{0.90}Eu_{0.10}F_{2.10}$	10	$\mathbf C$	5.920(1)	5.920(1)	5.920(1)	207.48(8)
4	$Pb_{0.85}Eu_{0.15}F_{2.15}$	15	$\mathbf C$	5.903(0)	5.903(0)	5.903(0)	205.66(2)
5	${\rm Pb_{0.80}Eu_{0.20}F_{2.20}}$	20	$\mathbf C$	5.890(1)	5.890(1)	5.890(1)	204.29(3)
6	$Pb_{0.75}Eu_{0.25}F_{2.25}$	25	$\mathbf C$	5.881(2)	5.881(2)	5.881(2)	203.4(1)
7	$Pb_{0.70}Eu_{0.30}F_{2.30}$	30	$\mathbf C$	5.875(1)	5.875(1)	5.875(1)	202.75(6)
			${\bf R}$	a			
8	$Pb_{0.65}Eu_{0.35}F_{2.35}$	35	$\mathbf C$	$\rm{a}$			$\rm{a}$
			$\mathbb{R}$	4.134(1)	4.134(1)	10.126(1)	149.84(3)
9	$Pb_{0.60}Eu_{0.40}F_{2.40}$	40	$\mathbf R$	4.132(1)	4.132(1)	10.119(1)	149.62(3)
				$\#4.125(1)$	60.17(1)		49.84(2)
10	$Pb_0$ 55 Eu <sub>0 45</sub> F <sub>2 45</sub>	45	$\mathbb{R}$	4.129(1)	4.129(1)	10.120(2)	149.62(3)
			$\mathbf O$	a			
11	$Pb_{0.50}Eu_{0.50}F_{2.50}$	50	$\mathbb{R}$	4.127(1)	4.127(1)	10.114(1)	149.19(4)
			$\mathbf O$	6.611(5)	7.034(5)	4.390(3)	204.2(2)
12	$Pb_{0.45}Eu_{0.55}F_{2.55}$	55	$\mathbb{R}$	4.127(1)	4.127(1)	10.111(1)	149.14(3)
			$\mathcal{O}$	6.618(3)	7.027(3)	4.391(2)	204.2(2)
13	$Pb_{0.40}Eu_{0.60}F_{2.60}$	60	$\mathbb{R}$	4.130(1)	4.130(1)	10.119(3)	149.48(7)
			$\mathbf O$	6.621(3)	7.029(3)	4.396(2)	204.6(2)
14	$Pb_{0.35}Eu_{0.65}F_{2.65}$	65	$\mathbf R$	4.129(1)	4.129(1)	10.117(2)	149.39(9)
			$\mathcal{O}$	6.615(3)	7.025(3)	4.391(2)	204.1(2)
15	$Pb_{0.30}Eu_{0.70}F_{2.70}$	70	$\mathbf R$	4.130(1)	4.130(1)	10.118(3)	149.49(7)
			$\mathcal{O}$	6.619(3)	7.026(3)	4.391(2)	204.2(2)
17	$Pb_{0.25}Eu_{0.75}F_{2.75}$	75	$\mathbb{R}$	4.135(2)	4.135(2)	10.121(6)	149.90(15)
			$\mathbf O$	6.622(2)	7.031(3)	4.396(2)	204.7(1)
19	$Pb_{0.20}Eu_{0.80}F_{2.80}$	80	$\mathbb{R}$	4.134(1)	4.134(1)	10.125(2)	149.86(6)
			$\mathbf O$	6.622(4)	7.032(3)	4.398(2)	204.8(1)
21	$Pb_{0.15}Eu_{0.85}F_{2.85}$	85	$\mathbb{R}$	4.130(1)	4.130(1)	10.113(2)	149.42(6)
			$\mathcal{O}$	6.618(2)	7.028(3)	4.393(2)	204.3(1)
24	$Pb_{0.10}Eu_{0.90}F_{2.90}$	90	$\mathbb{R}$	4.127(2)	4.127(2)	10.139(5)	149.55(14)
			$\mathcal{O}$	6.620(1)	7.015(2)	4.394(1)	204.1(1)
25	$Pb_{0.05}Eu_{0.95}F_{2.95}$	95	$\mathbf R$	a			
			$\mathcal{O}$	6.623(1)	7.019(2)	4.397(1)	204.4(1)
25	$Pb_{0.00}Eu_{1.00}F_{3.00}$	100	$\mathcal{O}$	6.626(1)	7.024(1)	4.401(1)	204.8(1)

 $C =$ Cubic (fluorite) type, R = Rhombohedral (Hexagonal settings),  $^{\#}$  = Rhombohedral (Rhombohedral settings), O = EuF<sub>3</sub> (orthorhombic YF<sub>3</sub>-type).<br><sup>a</sup> Corresponding phases were not refined due to very insignificant in

The unit cell parameters of the saturated fluorite type solid solution limits are,  $5.895(2)$  Å (for  $Pb_{0.70}Nd_{0.30}F_{2.30}$ , 5.881(2) Å (for  $Pb_{0.75}Eu_{0.25}F_{2.25}$ ) and 5.874(2) A (for  $Pb_{0.85}Er_{0.15}F_{2.15}$ ) as against that of 5.942(2) A for PbF<sub>2</sub>. A typical plot of variation of unit cell parameter of the fluorite-type solid solution with composition indicating the lattice contraction is shown in [Fig. 2.](#page-6-0) In the solid solution formation of  $MF_2-M'F_3$ , two significant but opposite factors, namely average cation radius and the inter-anionic repulsions, govern the unit cell dimension. Since the radii of the rare-earth ions in eight-fold coordination (ionic radii:  $Nd^{3+} = 1.11$ ,  $Eu^{3+} = 1.07$  and  $Er^{3+} = 1.00 \text{ Å}$ ) is quite smaller to Pb<sup>2+</sup> ion (radius 1.29 Å), the average ionic radius of the metal ion sites usually decreases. However, the unit cell of the solid solution lattice contains excess of the fluoride ions, which tend to dilate the unit cell due to electrostatic repulsion. The overall effect of these two opposite factors decides the dilation or contraction of the lattice.

In the earlier study of the  $PbF_2-YF_3$  system the lattice contraction was observed in the solid solution region [\[16\]](#page-11-0). The solid solution formation in  $BaF_2-MF_3$  [\[21,24–](#page-11-0) [26\]](#page-11-0) always causes the lattice contraction whereas that of the CaF<sub>2</sub>-M'F<sub>3</sub> ( $M' = Y^{3+}$  and Nd<sup>3+</sup>) system always causes lattice expansion [\[27,30\]](#page-11-0). In the present study, all the three systems show the lattice contraction, which implies that the decrease in the average cation radius dominates over the expansion caused by the inter-anion repulsion.

In the present study the typical solid solubility limit of  $NdF_3$ , EuF<sub>3</sub> and ErF<sub>3</sub> in PbF<sub>2</sub> is found to be 30, 25 and 15-mol%, respectively. In  $PbF_2-YF_3$  system, Reau et al. [\[11\]](#page-11-0) have observed 39 mol% as the solid solubility limit in the cubic  $PbF_2$  at about 885°C, which decreases to about 13-mol% at  $550^{\circ}$ C. From the interpolation of these values, the expected solubility limit of  $YF_3$  in  $PbF_2$ should be about  $22$ -mol% at  $650^{\circ}$ C. In the study of  $PbF_2-YF_3$  system (annealed at 700°C for 3 h) shows a

Table 3 Nominal compositions and their phase relations in  $Pb_{1-x}Er_xF_{2+x}$ 

S. No.	Nominal composition	mol% of $ErF_3$	Phase $(s)$ present	$a(\AA)$	$b(\AA)$	$c(\AA)$	$V(\AA)^3$
$\mathbf{1}$	$Pb_{1.00}Er_{0.00}F_{2.00}$	$\boldsymbol{0}$	$\mathbf C$	5.943(1)	5.943(1)	5.943(1)	209.90(4)
2	$Pb_{0.95}Er_{0.05}F_{2.05}$	5	$\mathbf C$	5.916(1)	5.916(1)	5.916(1)	207.06(7)
3	$Pb_{0.90}Er_{0.10}F_{2.10}$	10	$\mathbf C$	5.900(0)	5.900(0)	5.900(0)	205.34(2)
4	$Pb_{0.85}Er_{0.15}F_{2.15}$	15	$\mathsf{C}$	5.874(2)	5.874(2)	5.874(2)	202.71(9)
5	$Pb_{0.80}Er_{0.20}F_{2.20}$	20	$\mathbf C$	5.864(1)	5.864(1)	5.864(1)	201.65(4)
			$\mathbb{R}$	a	$\rm{a}$	$\mathbf{a}$	
6	$Pb_{0.75}Er_{0.25}F_{2.25}$	25	$\mathsf{C}$	5.874(1)	5.874(1)	5.874(1)	202.68(3)
			$\mathbb{R}$	4.076(1)	4.076(1)	10.003(4)	143.95(8)
7	$Pb_{0.70}Er_{0.30}F_{2.30}$	30	C	5.878(1)	5.878(1)	5.878(1)	203.06(6)
			${\bf R}$	4.075(1)	4.075(1)	9.998(4)	143.79(9)
8	$Pb_{0.65}Er_{0.35}F_{2.35}$	35	$\mathbf C$	5.878(1)	5.878(1)	5.878(1)	203.06(5)
			$\mathbf R$	4.083(1)	4.083(1)	10.013(3)	144.53(8)
9	$Pb_{0.60}Er_{0.40}F_{2.40}$	40	$\mathbb{R}$	4.078(1)	4.078(1)	10.006(2)	144.12(7)
				$4.086(1)^{\#}$	59.87(2)		48.08(3)
10	$Pb_{0.55}Er_{0.45}F_{2.45}$	45	$\mathbf T$	4.064(1)	4.064(1)	5.811(2)	96.00(4)
11	$Pb_{0.50}Er_{0.50}F_{2.50}$	50	T	4.046(1)	4.046(1)	5.796(2)	94.86(5)
			$\mathcal{O}$	$\mathbf{a}$			
12	$Pb_{0.45}Er_{0.55}F_{2.55}$	55	$\mathbf T$	4.050(1)	4.050(1)	5.803(2)	95.19(5)
			$\mathcal O$	a			
13	$Pb_{0.40}Er_{0.60}F_{2.60}$	60	T	4.051(1)	4.051(1)	5.802(2)	95.21(6)
			$\mathcal{O}$	6.343(4)	6.846(6)	4.397(3)	190.9(2)
14	$Pb_{0.35}Er_{0.65}F_{2.65}$	65	T	4.050(1)	4.050(1)	5.809(2)	95.29(4)
			$\mathbf O$	6.335(3)	6.845(5)	4.406(3)	191.2(2)
15	$Pb_{0.30}Er_{0.70}F_{2.70}$	70	T	4.046(1)	4.046(1)	5.796(1)	94.89(3)
			$\mathcal{O}$	6.342(3)	6.840(4)	4.382(3)	190.1(2)
17	$Pb_{0.25}Er_{0.75}F_{2.75}$	75	T	4.046(2)	4.046(2)	5.824(3)	95.35(8)
			$\mathcal{O}$	6.332(5)	6.842(7)	4.397(4)	190.5(3)
19	$Pb_{0.20}Er_{0.80}F_{2.80}$	$80\,$	T	4.037(3)	4.037(3)	5.836(4)	95.1(1)
			$\mathcal{O}$	6.333(2)	6.832(3)	4.383(2)	189.6(1)
21	$Pb_{0.15}Er_{0.85}F_{2.85}$	85	T	4.043(5)	4.043(5)	5.82(2)	95.1(4)
			$\mathcal{O}$	6.343(1)	6.840(1)	4.381(1)	190.1(0)
24	$Pb_{0.10}Er_{0.90}F_{2.90}$	90	T	4.091(6)	4.091(6)	5.81(2)	94.9(4)
			$\mathcal{O}$	6.341(1)	6.837(2)	4.381(1)	190.0(1)
25	$Pb_{0.05}Er_{0.95}F_{2.95}$	95	$\mathbf T$	a			
			${\rm O}$	6.353(2)	6.853(3)	4.394(2)	191.3(1)
25	$Pb_{0.00}Er_{1.00}F_{3.00}$	100	$\mathbf{O}$	6.354(1)	6.855(2)	4.395(1)	191.4(1)

 $C = C$ ubic (fluorite) type,  $R = R$ hombohedral (Hexagonal setting)  $# = R$ hombohedral (Rhombohedral settings), T = Tetragonal, O = Er $F_3$ (orthorhombic  $YF_3$ -type).

<sup>a</sup> Corresponding phases were not refined due to very insignificant intensities of reflections.

solubility limit of about 22-mol% of  $YF_3$  [\[16\].](#page-11-0) Due to the similarity in the ionic radii of  $Er^{3+}$  and  $Y^{3+}$ , it is expected that  $Erf_3$  should have similar solid solubility limit. The present observed solubility limit of  $Erf_3$  in PbF<sub>2</sub> is still lower than the values reported for  $PbF_2$ –  $YF_3$  system [\[11\]](#page-11-0). Dib et al. [\[12\]](#page-11-0) concluded the solid solubility limit of  $YF_3$  is about 17-mol% in spite of long annealed sample at  $400-600^{\circ}$ C. The authors also reported the solubility limit to be about 29-mol% at  $800^{\circ}$ C. The present observed value agrees with the corresponding values reported earlier  $[12]$  for  $YF_3$ . The solid solution behavior of the present study is closely similar to that reported for polycrystalline phase prepared by Mortier et al. [\[9\]](#page-11-0) by slowly cooling the melt of the  $PbF_2-ErF_3$  compositions. However, the higher solubility of  $Erf_3$  in PbF<sub>2</sub> in glass matrix is due to the partial oxygen incorporation from the oxy-

fluoride environment. The solid solubility limit of  $NdF_3$  in PbF<sub>2</sub> lattice (30 mol%) is more close to that in BaF<sub>2</sub> ( $\sim$ 35 mol%) [\[29\],](#page-11-0) but, it is lower than that in  $\text{SrF}_2$  (40 mol%) and  $\text{CaF}_2$  (45 mol%) lattices [\[30\]](#page-11-0). Similarly, the observed solubility limit of  $EuF_3$  in  $PbF_2$  is also close to that in  $BaF_2$  lattice [\[24\]](#page-11-0). The lower solubility values in the present case compared to that of  $BaF<sub>2</sub>-M'F<sub>3</sub>$   $(M'=Nd<sup>3+</sup>, Eu<sup>3+</sup>$  and  $Er<sup>3+</sup>)$  systems [\[24,28,29\],](#page-11-0) might be due to the low annealing temperature and shorter annealing time in the case of present investigation involving  $PbF<sub>2</sub>$ .

The XRD patterns of the nominal compositions  $Pb_{0.70}Eu_{0.30}F_{2.30}$  and  $Pb_{0.65}Eu_{0.35}F_{2.35}$  appear similar to typical fluorite-type phases, however, the presence of some weak reflections at  $2\theta \sim 25^{\circ}$ ,  $34^{\circ}$ ,  $36^{\circ}$ ,  $38^{\circ}$ ,  $40^{\circ}$ indicates either some sort of ordering in the fluorite-type lattice or appearance of some other phase. Besides, the

<span id="page-5-0"></span>Table 4 Summary of the various phases identified in the  $PbF_2-MF_3$  ( $M' = Nd^{3+}$ , Eu<sup>3+</sup> and Er<sup>3+</sup> systems)

S. No.	Nominal composition	mol% of $M/F_3$	Phases identified			
			$M/F_3 = NdF_3$	EuF <sub>3</sub>	ErF <sub>3</sub>	
	$Pb_{1.00}M'_{0.00}F_{2.00}$	$\theta$	$\mathbf F$	F	$\mathbf F$	
	$Pb_{0.95}M'_{0.05}F_{2.05}$	、	F	F	$\mathbf{F}$	
3	$Pb_{0.90}M_{0.10}'F_{2.10}$	10	$\boldsymbol{\mathrm{F}}$	F	$\mathbf{F}$	
	$Pb_{0.85}M'_{0.15}F_{2.15}$	15	F	F	${\bf F}$	
	$Pb_{0.80}M'_{0.20}F_{2.20}$	20	F	F	$F + R$	
6	$Pb_{0.75}M'_{0.25}F_{2.25}$	25	F	F	$F + R$	
	$Pb_{0.70}M'_{0.30}F_{2.30}$	30	F	$F + R$	$F + R$	
8	$Pb_{0.65}M'_{0.35}F_{2.35}$	35	$F + H$	$F + R$	$F + R$	
9	$Pb_{0.60}M'_{0.40}F_{2.40}$	40	$F + H$	R	R	
10	$Pb_{0.55}M'_{0.45}F_{2.55}$	45	$F + H$	$R + O$	T	
11	$Pb_{0.50}M'_{0.50}F_{2.50}$	50	$F + H$	$R + O$	T	
12	$Pb_{0.45}M'_{0.55}F_{2.55}$	55	$F + H$	$R + O$	$T + O$	
13	$Pb_{0.40}M'_{0.60}F_{2.60}$	60	$F + H$	$R + O$	$T+O$	
14	$Pb_{0.35}M'_{0.65}F_{2.65}$	65	$F + H$	$R + O$	$T+O$	
15	$Pb_{0.30}M'_{0.70}F_{2.70}$	70	$F + H$	$R + O$	$T + O$	
16	$Pb_{0.25}M'_{0.75}F_{2.75}$	75	$F + H$	$R + O$	$T+O$	
17	$Pb_{0.20}M'_{0.80}F_{2.80}$	80	$F + H$	$R + O$	$T+O$	
18	$Pb_{0.15}M'_{0.85}F_{2.85}$	85	$F + H$	$R + O$	$T+O$	
19	$Pb_{0.10}M'_{0.90}F_{2.90}$	90	$F + H$	$R + O$	$T + O$	
20	$Pb_{0.05}M'_{0.95}F_{2.95}$	95	$F + H$	$R + O$	$T+O$	
21	$Pb_{0.00}M'_{1.00}F_{3.00}$	100	H	$\Omega$	$\mathcal{O}$	

C=Cubic (fluorite) type, H=NdF<sub>3</sub> (hexagonal tysonite type), R=Rhombohedral, T=Tetragonal, O=ErF<sub>3</sub> or EuF<sub>3</sub> (orthorhombic YF<sub>3</sub> type).

splitting of reflections at  $2\theta \sim 44^{\circ}$ , 52° suggests distortion in the fluorite lattice. The weak reflections become more prominent at the nominal composition  $Pb_{0.60}Eu_{0.40}F_{2.40}$ . A comparison of these XRD patterns to the similar compositions in  $BaF_2-ErF_3$  or  $YF_3$  [\[24,28,31\]](#page-11-0),  $BaF<sub>2</sub>NdF<sub>3</sub>$  [\[29,32\]](#page-11-0) or PbF<sub>2</sub>-YF<sub>3</sub> [\[16,21\]](#page-11-0) systems suggests a rhombohedral ordering of the fluorite lattice in the present case also. All these systems contain rhombohedral phase with ideal composition  $M_4^{2+}M_3^{3+}F_{17}$  compositions. This phase was reported to exist in a narrow range of compositions, viz.  $40-44 \,\mathrm{mol}$ % of YF<sub>3</sub> [\[11\]](#page-11-0). The ideal composition of this rhombohedral phase should be  $Pb_4Eu_3F_{17}$ . A comparison of the XRD patterns of the nominal composition  $Pb_{0.70}Eu_{0.30}F_{2.30}$ ,  $Pb_{0.65}Eu_{0.35}F_{2.35}$  and  $Pb_{0.60}Eu_{0.40}F_{2.40}$  shows that all the observed reflections in the former two compositions are broadened significantly. A careful observation of the peak shape of intense reflections shows that the broadened reflections are nothing but convolution of the peaks arising from two different phases. However, it needs to be mentioned here that any clear spilt reflections attributable to the rhombohedral phase could not be observed in the  $PbF_2$ –EuF<sub>3</sub> system. The unit cell parameters of  $Pb_{0.60}Eu_{0.40}F_{2.40}$  were determined by analogy to the corresponding compositions, namely,  $Ba_{0.60}Eu_{0.40}F_{2.40}$  and  $Pb_{0.60}Er_{0.40}F_{2.40}$  like phases. The XRD pattern for nominal composition  $Pb_{0.55}Eu_{0.45}F_{2.45}$ shows the presence of orthorhombic  $EuF_3$ . The XRD pattern of nominal composition  $Pb_{0.60}Er_{0.40}F_{2.40}$  in  $PbF_2-ErrF_3$  system shows similar kind of weak reflec-

tions. This indicates that the ordered phases observed in both the systems are similar. The typical observed reflections for  $Pb_{0.60}Eu_{0.40}F_{2.40}$  and  $Pb_{0.60}Er_{0.40}F_{2.40}$ , excluding the weak reflections, could be indexed on a rhombohedral lattice with unit cell parameters:  $a =$ 4.132(1) and  $c = 10.119(1)$  Å, and  $a = 4.078(1)$  and  $c = 10.006(3)$  Å, respectively. By the comparison of the XRD patterns of the present phases  $(Pb_{0.60}Eu_{0.40}F_{2.40})$ and  $Pb_{0.60}Er_{0.40}F_{2.40}$  with those of  $Pb_4Y_3F_{17}$  [\[21\]](#page-11-0)  $Ba_4Eu_3F_{17}$  [\[31\]](#page-11-0) and  $Ba_4Y_3F_{17}$  [\[34\],](#page-11-0) a larger rhombohedral unit cell and space group  $R - 3$  (No. 148) is proposed. This larger unit cell represents the superstructure of the former smaller (basis cell) unit cell. The typical basis and superstructure unit cell parameters are:

 $Pb_{0.60}Eu_{0.40}F_{2.40}$ 

$$
a = 4.132(1), c = 10.119(1) \text{ Å and } V = 149.62(3) \text{ Å}^3
$$
  
(basis structure);  
 $a = 10.928(3), c = 20.278(11) \text{ Å and } V = 2097.0$   
(1.3)  $\text{Å}^3$  (superstructure).

 $Pb_{0.60}Er_{0.40}F_{2.40}$ 

 $a = 4.078(1)$ ,  $c = 10.006(3)$  Å and  $V = 144.12(7)$  Å<sup>3</sup> (basis structure);  $a = 10.804(2), c = 19.962(6)$  Å and  $V = 2017.9(9)$  Å<sup>3</sup> (superstructure).

The typical miller indices of the observed reflections for  $Pb_{0.60}Eu_{0.40}F_{2.40}$  and  $Pb_{0.60}Er_{0.40}F_{2.40}$ , in both the

<span id="page-6-0"></span>

Fig. 1. Powder XRD patterns of  $PbF_2$  and various solid solutions; A:  $\alpha$ -PbF<sub>2</sub> (orthorhombic), B:  $\beta$ -PbF<sub>2</sub> (cubic), C: Pb<sub>0.70</sub>Nd<sub>0.30</sub>F<sub>2.30</sub>, D:  $Pb_{0.75}Eu_{0.25}F_{2.25}$  and E:  $Pb_{0.85}Er_{0.15}F_{2.15}$ .

hexagonal and rhombohedral settings are summarized in Tables 5 and 6, respectively. The observed powder XRD patterns of these two nominal compositions are shown in [Fig. 3](#page-7-0). These basis and superstructure unit cells are, however, closely related among themselves and also to the parent fluorite lattice in an approximate relation as:  $a_{\text{super}} = \sqrt{7 \times a_{\text{sub}}}$  and  $c_{\text{super}} = 2 \times c_{\text{sub}}$ ;  $a_{\text{sur}}$  $b=\sqrt{2} \times af$  and  $c_{sub}=\sqrt{3} \times a_f$  (the subscripts super and sub represent the superstructure and basis structure lattice parameters and the subscript f is used to indicate for parent fluorite unit cell). Such relations between rhombohedral and fluorite unit cells have been explained in several reports [\[19,33,34\].](#page-11-0)

To characterize the exact nature of the rhombohedral phase, ideal stoichiometric composition  $Pb_4E_r$ <sub>17</sub> was prepared under similar experimental conditions. A detailed XRD analysis was carried out to elucidate the crystal structure of this phase. The powder XRD pattern shows a clear doublet like feature at  $2\theta \sim 44^{\circ}$  (corresponding to rhombohedral distortion of 220 reflection of parent fluorite lattice). Besides, this phase contains a number of weak reflections, at  $2\theta \sim 21$ , 24, 25, 34, 35, 36,



Fig. 2. Variation of unit cell volume as a function of  $M'F_3$  content in the fluorite-type solid solution.

Table 5 Observed and calculated reflections for  $Pb_{0.60}Eu_{0.40}F_{2.40}$ 

S. No.	$d_{\text{(obs)}}$ (A)	$I/I_0$ $($ %)	$d_{\text{(cal)}}$ $(A)$ (1)	hkl (1)	hkl(2)	h k l (3)
1	3.738	3	3.728	105	221	
$\overline{2}$	3.529	$\overline{2}$	3.522	211	$2 - 10$	
3	3.376	100	3.373	212	$21 - 1$	101
$\overline{4}$	2.922	45	2.923	214	310	102
5	2.602	1	2.603	311	$2 - 21$	
6	2.540	$\overline{2}$	2.541	312	$3 - 10$	
7	2.470	1	2.471	207	331	
8	2.352	$\overline{2}$	2.350	401	$3 - 1 - 1$	
9	2.251	3	2.251	217	421	
10	2.124	1	2.125	226	420	
11	2.066	64	2.065	410	$3 - 2 - 1$	104
12	2.043	$\overline{2}$	2.044	405	$33 - 1$	
13	1.762	54	1.762	416	$43 - 1$	113
14	1.737	3	1.737	327	520	
15	1.686	$\overline{2}$	1.687	424	$42 - 2$	006
16	1.461	8	1.461	428	620	204

Typical unit cell parameters: (1). Hexagonal (supercell):  $a = 10.928(3)$ ,  $c = 20.278(11)$  Å and  $V = 2097.0(1.3)$  Å<sup>3</sup>; (2). Rhomb. (supercell):  $a = 9.245(3)$  Å,  $\alpha = 72.48(3)$ °, and  $V = 699.0(4)$  Å<sup>3</sup>; (3). Hexagonal (basiscell):  $a = 4.132(1)$ ,  $c = 10.119(1)$  Å and  $V = 149.62(3)$  Å<sup>3</sup>. Corresponding rhombohedral cell:  $a = 4.125(1)$ ,  $\alpha = 60.17(1)$  and  $V = 49.84(2)$  Å.

38, 40, etc. (can be seen from inset of [Fig. 4](#page-7-0)), which indicate the superstructure formation in the rhombohedral lattice. The observed powder profile was refined by Rietveld method using the Fullprof 2000 software package [\[35\]](#page-11-0). The initial position coordinates for various

<span id="page-7-0"></span>Table 6 Observed and calculated reflections for  $Pb_{0.60}Er_{0.40}F_{2.40}$ 

			S. No. $d_{(obs)}$ (A) $I/I_0$ (%) $d_{(cal)}$ (A) (1) $hkl$ (1) $hkl$ (2)			hkl(3)
1	4.206	$\lt 1$	4.194	113	210	
$\overline{2}$	3.671	1	3.672	105	221	
3	3.487	2	3.482	211	$2 - 10$	
$\overline{4}$	3.332	100	3.333	212	$21 - 1$	101
5	2.886	45	2.885	214	310	102
6	2.503	$\overline{2}$	2.503	223	$31 - 1$	
$\overline{7}$	2.323	$\lt 1$	2.323	401	$3 - 1 - 1$	
8	2.217	3	2.218	009	333	
9	2.100	1	2.099	322	$3 - 21$	
10	2.042	45	2.042	410	$3 - 2 - 1$	104
11	2.037	35	2.039	218	431	110
12	1.740	42	1.740	416	510	113
13	1.713	1	1.714	229	531	
14	1.693	1	1.692	2011	533	
15	1.667	10	1.667	424	$42 - 2$	006
16	1.533	$\leq$ 1	1.534	431	$4 - 30$	
17	1.443	6	1.443	428	620	204

Typical unit cell parameters: (1). Hexagonal (supercell):  $a = 10.804(2)$ ,  $c = 19.962(6)$  Å and  $V = 2017.9(9)$  Å<sup>3</sup>; (2). Rhomb. (supercell):  $a =$ 9.121(3) $\AA$ ,  $\alpha = 72.64(3)^\circ$ , and  $V = 672.7(3) \AA^3$ ; (3). Hexagonal (basiscell):  $a = 4.078(1)$ ,  $c = 10.006(3)$  Å and  $V = 144.12(7)$  Å<sup>3</sup>.

Corresponding rhombohedral cell:  $a = 4.086(2)$ ,  $\alpha = 59.87(2)$  and  $V = 48.08(3)$  Å.



Fig. 3. Observed powder XRD pattern for nominal compositions  $Pb_{0.60}Eu_{0.40}F_{2.40}$  and  $Pb_{0.60}Er_{0.40}F_{2.40}$  (super-structure reflections are indicated by arrows).



Fig. 4. Observed and calculated XRD patterns of  $Pb_4Er_3F_{17}$ . The difference plot is given below the pattern. The typical possible Bragg reflections are indicated by the vertical marks below the Rietveld plot.

Table 7 Typical crystallographic data and refined parameters for  $Pb_4Er_3F_{17}$ 

$Pb_4Er_3F_{17}$
$25^{\circ}$ C
Rhombohedral, $R-3$ (No. 148)
10.8190 (2) and 19.9513 (8)
2022.4(1)
$0.075(7)$ , $-0.050(6)$ , $0.033(2)$
$0.011(1)$ and $0.29(1)$
$0.092(5)$ , $0.044(2)$
$10.1\%$ , 13.2% and 9.44%
1.97
6.5%

atoms and space group are taken from the reported crystal structure of  $Ba_4Y_3F_{17}$  [\[20\]](#page-11-0). The profile is fitted with pseudo-Voigt profile function. Initially scale and background are corrected with approximately accurate unit cell and profile parameters. The background is fitted with a fifth-order polynomial function. Further preferred orientation correction is applied using Rietveld function. The asymmetry correction is done with two-term asymmetry function. The refined unit cell parameters of  $Pb_4Er_3F_{17}$  are:  $a = 10.8190(2)$  and  $c = 19.9513(8)$  Å,  $V = 2022.44(1)$  Å<sup>3</sup>. The details of other refined parameters and residuals of refinements are given in Tables 7 and 8. The typical Rietveld refinement plot showing the observed and calculated diffraction pattern along with the difference plot is shown in Fig. 4. The insets in the figure indicate some of the weak super structure reflections and typical split reflection. The vertical marks at the bottom indicate Bragg positions of a large number of possible refection.

The crystal structure analysis of this phase shows two crystallographically different lead atoms and one distinct erbium atom (in the ratio of 6:18:18) in the unit cell. There are eight different kinds of fluorine atoms in the unit cell. Erbium atoms are coordinated with the

Table 8 Position coordinates of various atoms of  $Pb_4Er_3F_{17}$  in the unit cell

Atom	site	Occ.	$\mathcal{X}$	у	$\mathcal{Z}_{\mathcal{L}}$
P <sub>b</sub> 1	6с	1	$\theta$	$\theta$	0.2611(3)
Pb2	18f	1	0.2304(4)	0.0338(4)	0.0856(2)
Er1	18f	1	0.0866(4)	0.6128(3)	0.0785(2)
F1	18f	1	0.056(4)	0.786(3)	0.032(2)
F <sub>2</sub>	18f		0.430(4)	0.293(3)	0.112(2)
F <sub>3</sub>	18f	1	0.485(5)	0.096(3)	0.042(3)
F <sub>4</sub>	18f	1	0.207(3)	0.506(4)	0.039(1)
F <sub>5</sub>	18f	1	0.266(4)	0.383(2)	0.174(1)
F <sub>6</sub>	6с	1			0.134(4)
F7	3a		$\theta$	0	$\theta$
F8 <sup>a</sup>	18f	0.167	0.948	0.930	0.494

 $B_{\text{overall}} = 0.61(2) \text{ Å}^2.$ <br><sup>a</sup> Position coording

<sup>a</sup> Position coordinates of F8 atom is not included in the refinements. They are kept fixed at the given values.



Fig. 5. A typical  $Er_6F_{36+1}$  cluster of  $Pb_4Er_3F_{17}$ ,  $ErF_8$  polyhedra are shown and the inner smaller spheres indicate the F8 atoms.

eight fluorine atoms forming a square anti-prism. Six of the  $Erf_8$  square anti-prisms share the corners of one of their square face and form  $Er_6F_{36}$  cluster. The  $Er_6F_{36}$ cluster is the building block of many of the anion-excess fluorite related compounds. The Pb1 and Pb2 are 10 and 11 coordinated with the fluoride ions. The typical arrangements of all the atoms are similar to the reported structure of  $Ba_4Y_3F_{17}$  [\[20\]](#page-11-0) and  $Ba_4Er_3F_{17}$  [\[31\].](#page-11-0) The typical Er–F bonds range from 2.26 to 2.40 Å. The Pb1– F bond lengths range from 2.50 to  $2.72 \text{ Å}$ . The Pb2 exists as a highly distorted 11-coordinated polyhedron with bonds ranging from  $2.37$  to  $3.34$  Å. A representative  $Er_6F_{36}$  cluster is shown in Fig. 5. The F4 and F5 atoms of the  $Er_6F_{36}$  cluster form a cubo-octahedron. One additional F8 fluorine atom is distributed over the

18f sites inside the cubo-octahedron cluster, and thus the  $Er_6F_{36}$  cluster can be better explained as  $Er_6F_{37}$ cluster. It needs to be mentioned here that the F8 atom position is not refined in the Rietveld refinement cycles. The powder XRD pattern of the corresponding phase  $Pb_4Eu_3F_{17}$  is closely similar to the  $Pb_4Er_3F_{17}$ . The detailed XRD study of this phase is in progress and will be communicated separately.

In the  $PbF<sub>2</sub>NdF<sub>3</sub>$  system, beyond the solid solution limit, i.e., compositions subsequent to  $Pb_{0.70}Nd_{0.30}F_{2.30}$ show reflections attributable to  $NdF_3$ . This indicates that there are no other phases present in this system except the fluorite-type solid solution and  $NdF_3$  phases. Similarly, in  $PbF_2$ -EuF<sub>3</sub> system, compositions beyond the rhombohedral phase, i.e.,  $Pb_{0.55}Eu_{0.45}F_{2.55}$  and so on, show the presence of  $EuF_3$  reflections. From this observation, it can be inferred that no other phases, except the fluorite-type solid solution and rhombohedral phase, are observed in this system.

The XRD pattern of the nominal composition  $Pb_{0.55}Er_{0.45}F_{2.45}$ , which follows the rhombohedral ordered phase in  $PbF_2-ErrF_3$  system, shows the absence of all the weak reflections present in the nominal composition  $Pb_{0.60}Er_{0.40}F_{2.40}$ . The typical fluorite peak positions at  $2\theta \sim 31^{\circ}$  and  $52^{\circ}$  appear as doublets in the XRD pattern. In addition, the presence of weak reflections at  $2\theta \sim 34^{\circ}$  and 37° are additional features in the XRD pattern of this composition. A typical XRD pattern of  $Pb_{0.55}Er_{0.45}F_{2.45}$  is shown in Fig. 6. Thus, it was considered as a new phase different from the above explained fluorite related rhombohedral phase. This phase is quite similar to tetragonal [\[11\]](#page-11-0) and orthorhombically distorted tetragonal [\[16\]](#page-11-0) phases observed in  $PbF_2-YF_3$  system. A similar XRD pattern was also observed at the nominal composition  $Pb_{0.50}Er_{0.50}F_{2.50}$ . Beyond this nominal composition, the other compositions were found to contain reflections due to  $Erf_3$ . The observed reflections for the  $Pb_{0.55}Er_{0.45}F_{2.45}$  and



Fig. 6. Observed powder XRD pattern for nominal composition  $Pb_{0.55}Er_{0.45}F_{2.45}$  (super-structure reflections are indicated by arrows).

Table 9 Observed and calculated reflections for  $Pb_{0.55}Er_{0.45}F_{2.45}$ 

S. No.	$d_{\text{(obs)}}$ (A)	$I/I_0$ $(\%)$	$d_{\text{(cal)}}$ $(A)$ $(1)$	hkl (1)	$d_{\text{(cal)}}$ $(A)$ $(2)$	hkl (2)
1	3.953	$\lt 1$			3.958	101
$\overline{2}$	3.334	100	3.331	101	3.331	103
3	2.909	17	2.906	002	2.907	006
4	2.878	29	2.874	110	2.874	110
5	2.649	$\lt 1$			2.647	105
6	2.401	1			2.400	114
7	2.044	47	2.043	112	2.044	116
8	2.032	19	2.032	200	2.032	200
9	1.748	23	1.749	103	1.749	109
10	1.735	34	1.735	211	1.735	213
11	1.665	12	1.665	202	1.666	206
12	1.454	$\overline{4}$	1.453	004	1.454	0012
13	1.436	4	1.437	220	1.437	220

Typical unit cell parameters: (1)  $a = 4.064(1)$ ,  $c = 5.811(2)$  Å and  $V = 96.00(4)$  Å<sup>3</sup>; (2)  $a = 4.064(1)$ ,  $c = 17.442(4)$ Å and  $V = 288.1(1) \text{ Å}^3.$ 

 $Pb_{0.50}Er_{0.50}F_{2.50}$  excluding the weak reflections could be indexed on a tetragonal lattice (basis lattice). To include the weak reflections, the c-axis of the tetragonal unit cell had to be tripled. A list of the observed and calculated reflections for the nominal composition  $Pb_{0.55}Er_{0.45}F_{2.45}$ is given in Table 9. The typical unit cell parameters of the tetragonal phases observed in the compositions  $Pb_{0.55}Er_{0.45}F_{2.45}$  and  $Pb_{0.50}Er_{0.50}F_{2.50}$  are:

 $Pb_{0.55}Er_{0.45}F_{2.45}$ 

 $a = 4.064(1)$ ,  $c = 5.811(2)$  Å and  $V = 96.00(4)$  Å<sup>3</sup> (basis lattice);  $a = 4.064(1)$ ,  $c = 17.442(4)$  Å and  $V = 288.1(1)$  Å<sup>3</sup> (superstructure lattice).

 $Pb_{0.50}Er_{0.50}F_{2.50}$ 

 $a = 4.046(1)$ ,  $c = 5.796(2)$  Å and  $V = 94.86(5)$  Å<sup>3</sup> (basis lattice);  $a = 4.046(1)$ ,  $c = 17.386(6)$  Å and  $V = 284.5(1)$  Å<sup>3</sup> (superstructure lattice).

These unit cell parameters bear close relation to the parent fluorite unit cell. The typical relation between the unit cell parameters of the tetragonal unit cell and the parent fluorite unit cell are as:  $a_{t(basis)} \approx a_f/\sqrt{2}$  and  $c_{t(basis)} \approx a_f$  and the exact cell parameters are:  $a_t = a_{t(basis)}$ and  $c_t = 3 \times c_{t(basis)}$ , where the subscript 't' and 'f' indicate the tetragonal and fluorite unit cells, respectively. Reau et al. [\[11\]](#page-11-0) have reported a similar composition close to  $PbYF_5$  (i.e., at about 49 mol% of  $YF_3$ ) with a tetragonal unit cell having  $4.076(2)$  and  $17.400(5)$  Å, as a and c parameters, respectively. Earlier closely related tetragonal unit cells have been proposed for  $Pb_2YF_7$  $(a_t = 4.080(1)$  and  $c_t = 17.392(4)$  Å) [\[12\]](#page-11-0) and  $Ca_2YbF_7$  $(\sim 2 \times a_t$  and  $c_t$ ) type compositions [\[36\]](#page-11-0) (tetragonal unit cell parameters for  $Ca<sub>2</sub>YbF<sub>7</sub>$  are reported as: 8.673(0) and  $16.577(1)$  A).

The indices of the observed powder XRD pattern of  $Pb_{0.55}Er_{0.45}F_{2.45}$  (Table 9) suggests  $I4/mmm$  space group for this phase. Earlier Dib et al. [\[12\]](#page-11-0) have reported similar unit cell parameters for  $Pb_2YF_7$ composition, but they assigned space group I4 or  $I4/m$ . Ness et al. [\[36\]](#page-11-0) have proposed  $2 \times a_t$  and  $c_t$  as unit cell parameter for a closely similar composition  $Ca<sub>2</sub>YbF<sub>7</sub>$  in  $CaF<sub>2</sub>-YbF<sub>3</sub>$  system. They assigned space group  $I4/m$  for this structure. In this structure they have reported a randomization of several Ca and Yb atoms in the lattice. In their structural report they have proposed partial occupancy of Ca<sup>2+</sup>, Yb<sup>3+</sup> in 8h, 4e and 2b sites, with square anti-prism or cubical coordination polyhedra. The  $Ca^{2+}$  in 16*i* sites have a 10-coordinated polyhedron. A similar arrangement with 8h, 4e and 2b site with  $Er^{3+}$  and 16*i* for Pb<sup>2+</sup> is expected for the present composition. The present powder XRD data, however, do not show any indication for space group  $I4/m$ , hence, we could not use this model for our study. The exact structural arrangement of this phase will be carried out and will be reported subsequently.

A careful analysis of the XRD pattern of  $Pb_{0.50}Er_{0.50}F_{2.50}$  indicates the presence of a very small amount of  $Erf_3$ . The intensity of the reflections attributable to  $Erf_3$  increases in the subsequent compositions. This suggests that the tetragonal phase exists with slightly less than 50 mol% as observed by Reau et al. for  $PbF_2-YF_3$  [\[11\]](#page-11-0) system. All other following compositions yield a mixture of the tetragonal phase of the type  $Pb_{0.55}Er_{0.45}F_{2.45}$  and the leftover  $ErF_3$ .

It was also revealed that no  $PbF_2$  could be retained in any of the three rare-earth fluoride lattices. This was further verified from the determination of unit cell parameters of the rare-earth fluoride phases in the different nominal compositions. Earlier it was reported in Ba $F_2$ - $M'F_3$  (where  $M' = Y^{3+}$ ,  $Er^{3+}$ ,  $Eu^{3+}$ ) systems that no  $BaF_2$  can be incorporated into  $YF_3$ ,  $ErF_3$  and EuF<sub>3</sub> lattices [\[24,28\]](#page-11-0). The presently studied  $PbF_2$ –EuF<sub>3</sub> and  $PbF<sub>2</sub>$ –Er $F<sub>3</sub>$  systems also show similar results. But in the case of  $MF_2$ -NdF<sub>3</sub> ( $M = Ba^{2+}$ ,  $Sr^{2+}$  and  $Ca^{2+}$ ) systems, about 10-mol% of  $MF<sub>2</sub>$  could be retained in the NdF<sub>3</sub> lattice [\[29,30\]](#page-11-0). However, no PbF<sub>2</sub> could be incorporated into the  $NdF<sub>3</sub>$  lattice. Besides, no tysonitetype phase or  $Er<sub>2</sub>BaF<sub>8</sub>$  type phase was observed in these studied systems.

The summary of the phase relations in the three studied systems is shown as bar diagram in [Fig. 7.](#page-10-0) In each segment, the extreme left end indicates the fluoritetype solid solution and the extreme right end indicates the rare-earth fluoride lattice. A comparison of the three studied systems reveals that the fluorite-type solid solution is the only common feature in them. The rhombohedral ordered phase were observed both in the  $PbF_2$ –EuF<sub>3</sub> and  $PbF_2$ –ErF<sub>3</sub> systems, but not in the

<span id="page-10-0"></span>

Fig. 7. Summary of phase relations in  $Pb_{1-x}M'_{x}F_{2+x}$  systems (bar representation) F=Fluorite, R=Rhombohedral, T=Tetragonal Unmarked zones (biphasic) contain two neighboring phases.

 $PbF_2-NdF_3$  system. The tetragonal ordered phase is observed only in  $PbF_2-Err_3$  system.

In the earlier phase relation studies in  $MF_2-M'F_3$ systems, it was observed that the typical solid solution limit increases with the decrease in the difference in the ionic radii of the  $M^{2+}$  and  $M^{3+}$  cations [\[27,30\]](#page-11-0). A similar conclusion was also drawn in the present studied systems, i.e., the typical solid solution limit increases from  $PbF<sub>2</sub>$ –Er $F<sub>3</sub>$  to  $PbF<sub>2</sub>$ Nd $F<sub>3</sub>$  system, viz. 15–30 mol% with change in rare-earth ion from  $Er^{3+}$  to  $Nd^{3+}$ . The formation of the rhombohedral phase in  $PbF_2$ –EuF<sub>3</sub>,  $PbF_2-Err_3$  or  $PbF_2-YF_3$  systems indicates that the ionic radii of  $M^{2+}$  and  $M^{3+}$  plays a significant role in the formation of the rhombohedral ordered phase. Such rhombohedral phase was observed with  $NdF_3$  only when the counter cation is  $Ba^{2+}$ . From, these observations it can be suggested that the rhombohedral and other ordered phases are possible, only when there is a significant difference in the ionic radii of  $M^{2+}$  and  $M^{3+}$ . The formation of the tetragonal phase only in  $PbF_2-ErF_3$  and  $PbF_2-YF_3$  [\[16\]](#page-11-0) systems (within 45– 50 mol% of  $M/F_3$ ), suggests the ionic radii of the rareearth ion has an important role in its stabilization. However, the rhombohedral phase is observed in wide range of rare-earth ions. Fedorov et al. had reported the  $PbF_2-M'F_3$  ( $M'=Ho^{3+}$ ,  $Yb^{3+}$  and  $Sc^{3+}$ ) phase equilibria from the phase analysis of the quenched samples [\[15\]](#page-11-0). In all these phase equilibria they had not observed any tetragonal phase neither at 33 or 50-mol% of  $M/F_3$ . A comparison of the results obtained in the present study with those of Reau et al. [\[11\]](#page-11-0), Dib et al. [\[12\]](#page-11-0) and Fedorov et al. [\[15\]](#page-11-0) suggests the preparation conditions, namely, heating temperature, annealing time and cooling protocol also play equally important role in governing the phase equilibria. Except the study made by Reau et al., all other literature studies [\[11,15\]](#page-11-0) are based on the long annealed samples. Thus, at present it is concluded that besides the optimally different ionic radii of the guest and host ions, the short annealing conditions are ideal for the formation of such a tetragonal phase.

In any of these three systems,  $PbF_2$  did not show any solubility in the  $M'F_3$  lattices. However, in the earlier studies on  $MF_2$ -NdF<sub>3</sub> ( $M = Ca^{2+}$ ,  $Sr^{2+}$  and  $Ba^{2+}$ ) systems solubility of  $M^{2+}$  in NdF<sub>3</sub> was reported [\[29,30\]](#page-11-0).

This may be because of higher electropositive character of the alkaline-earth metals than lead. Thus, the solubility of  $M^{2+}$  in  $M'F_3$  lattice is not only governed by the radius of the metal ions but also by the nature of the metal ion.

The  $PbF_2-MF_3$  systems, more closely resemble with the Ba $F_2$ - $M'F_3$  system, despite the fact that ionic radius of  $Pb^{2+}$  is very close to that of  $Sr^{2+}$ . However, many differences between  $PbF_2 - M'F_3$  and  $BaF_2 - M'F_3$  systems are also observed, which are due to a considerable difference between ionic radii and electro-positive character difference between the alkaline earth metal ions and  $Pb^{2+}$ . Thus, the ionic radii of the  $M^3$  cation has a governing role in the formation of the ordered phases or deciding width of solid solution in  $M_{\rm P2}$ - $M_{\rm P3}$ phase equilibria. Smaller difference between the ionic radii facilitates the solid solution formation whereas the larger difference leads to the cations segregation which results in ordered structure formation.

## 4. Conclusions

From the foregoing, the phase relations in  $PbF_2$ –  $M'F_3$   $(M' = Nd^{3+}, Eu^{3+}$  and  $Er^{3+}$ ) under short annealed and slow cooled conditions are established. The typical solid solution limit of  $NdF_2$ ,  $EuF_3$  and  $ErF_3$ in  $PbF_2$  are 30, 25 and 15-mol%, respectively. A rhombohedral fluorite related ordered phased was observed in  $PbF_2$ –EuF<sub>3</sub> and  $PbF_2$ –ErF<sub>3</sub> systems near the composition  $Pb_{0.60}M_{0.40}F_{2.40}$ . A tetragonal fluorite related ordered phase is observed only in  $PbF_2-ErF_3$ system. No tysonite or tysonite related phases are observed in these systems. In addition, no solubility of the  $PbF_2$  in the rare-earth fluorides is observed in the present study.

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